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# Reply to: Insufficient evidence for ageing in protein dynamics

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REPLYING TO I. Goychuk & T. Pöschel Nature Physics https://doi.org/10.1038/s41567-021-01269-1 (2021)

Reference <sup>1</sup> states that we<sup>2</sup> claimed that internal motions in single protein molecules exhibit ageing over 13 decades of time. In contrast, our primary conclusion, as expressed in the title, was that over these timescales the dynamics of single protein molecules is non-equilibrium and self-similar<sup>2</sup>. Notwithstanding, we demonstrate here that protein dynamics does indeed exhibit ageing according to the criteria of ref. <sup>1</sup>.

Reference <sup>1</sup> claims that to adequately describe the ageing process a two-time point correlation function should be calculated. In Fig. 1a, we plot the following two-time correlation function using the T=17-µs-simulation-length trajectory from ref. <sup>2</sup> of the protein phosphoglycerate kinase (PGK):

$$K(t_{ag}, t_{ag} + \Delta; T) = \frac{1}{T - t_{ag} - \Delta} \int_{0}^{T - t_{ag} - \Delta} \delta R(t_{ag} + t') \, \delta R(t_{ag} + t' + \Delta) \, dt'$$
(1)

where  $\Delta$  is the lag time, *t* is the time,  $t_{ag}$  is the ageing time and  $\delta R$  is the deviation of the interdomain distance of PGK from its time-averaged value. In the corresponding equation (3) of ref.<sup>1</sup>, *R* is used instead of  $\delta R$ , which renders the interdomain correlation function meaningless as no appreciable decay is present. Furthermore, the literature cited in ref.<sup>1</sup> (ref.<sup>3</sup>) also defines wide-sense stationarity (that is, in the mean-square sense) in terms of  $\delta R$ .

As shown in Fig. 1a,  $K(t_{ag}, t_{ag} + \Delta; T)$  shifts upon changing  $t_{ag}$ , hence, according to ref.<sup>1</sup>, demonstrating ageing. Further confirmation of ageing was obtained by carrying out 100 independent molecular dynamics simulations of PGK, each of T = 100 ns, and plotting the ensemble- and time-averaged mean square atomic displacement,  $\langle \overline{\delta^2(\Delta, T)} \rangle$ , as a function of *t* (that is,  $T - t_{ag}$ ) at fixed  $\Delta$  (Fig. 1b). An appreciable decay of  $\langle \overline{\delta^2(\Delta, T)} \rangle$  with *t* is observed, and is direct evidence of ageing<sup>4,5</sup>.

In Fig. 2a of ref.<sup>2</sup> the time-averaged (not ensemble-averaged) mean square atomic displacement,  $\delta^2(\Delta, T)$  is shown for different *t*. Reference <sup>1</sup> states that Fig. 2a of ref.<sup>2</sup> was used to claim ageing and the absence of ergodicity. However, neither ageing nor non-ergodicity were claimed from this plot. Instead, the conclusion from Fig. 2a–c of ref.<sup>2</sup> was the presence of strong non-stationarity.

 $\Delta \ll t$  is stipulated in ref.<sup>1</sup> as a condition for statistical validity. In Fig. 2a of ref.<sup>2</sup> the 10 ns simulation line deviates from that of the 100 ps simulation for  $\Delta > 1$  ps (and not  $\Delta > 30$  ps as stated in ref.<sup>1</sup>). Further,  $\overline{\delta^2(\Delta, T)}$  from the 17 µs simulation deviates from that of 500 ns for  $\Delta > 100$  ps. Therefore, the  $t/\Delta$  are  $\sim 10^2$  and  $\sim 10^4$ , respectively, satisfying the requirement of ref.<sup>1</sup>. Also, an overlap of  $\overline{\delta^2(\Delta, T)}$  at different *t* at small  $\Delta$ , as seen in Fig. 2a of ref.<sup>2</sup>, arising from stationary noise, exists for a confined noisy continuous-time random walk<sup>5,6</sup>, which is the non-ergodic model used to interpret the simulation data in ref.<sup>2</sup>.

Figure 1 here, as well as other pieces of evidence in ref.<sup>2</sup>, satisfy the conditions for ageing claimed in ref.<sup>1</sup>. However, ref.<sup>4</sup> shows that, even if two-time correlation functions such as equation (1) do exhibit non-stationarity, this does not prove breaking of time translational invariance. Indeed, according to equation (1) (and equation (3) in ref.<sup>1</sup>) even ergodic dynamics, if evolving from a non-stationary initial condition, exhibits transient ageing<sup>4</sup>. Using rigorous mathematics ref.<sup>4</sup> instead shows that the dynamics of PGK does indeed exhibit breaking of time translational invariance. Moreover, ref.<sup>4</sup> shows that all systems tracking low-dimensional observables projected from the full system phase space as a function of time for which (1) the projection renders the reduced dynamics non-Markovian and (2) the observable is not prepared in, or initially sampled from and averaged over, a stationary distribution always exhibit non-equilibrium dynamic time asymmetry (DTA). DTA sports characteristics commonly associated with ageing. However, DTA and the definition of ageing adopted by the theoretical glass physics community are distinguishable: the latter requires that the relaxation time be beyond the longest times accessible to experiment or simulation, which itself typically requires that the relaxation time increase exponentially with system size<sup>7-11</sup>.

In contrast to the claims in ref.<sup>1</sup>, the results in ref.<sup>2</sup>, together with the above analysis, the analysis in ref.<sup>4</sup> and experimental results from single-molecule spectroscopic time series published over the intervening 5 yr (refs.<sup>12,13</sup>) since ref.<sup>2</sup> was published, have led to the unequivocal conclusion that the internal motions of a single protein are non-equilibrium, self-similar and, according to the criteria of ref.<sup>1</sup>, both non-ergodic and ageing. More generally, DTA is ubiquitous in complex materials and biological systems, and must surely change the way in which many experiments and simulations are interpreted.

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**Fig. 1** Demonstration of ageing in molecular dynamics of PGK. a, Two-time autocorrelation function defined in equation (1). **b**, Ensemble- and time-averaged mean square displacement as a function of t at fixed  $\Delta$ .

#### **Online content**

Any methods, additional references, Nature Research reporting summaries, source data, extended data, supplementary information, acknowledgements, peer review information; details of author contributions and competing interests; and statements of data and code availability are available at https://doi.org/10.1038/ s41567-021-01270-8.

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#### Author contributions

J.L. and L.H. performed the calculations in Fig. 1. All authors planned the research, analysed the results and wrote the manuscript.

#### **Competing interests**

The authors declare no competing interests.

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#### **Additional information**

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